## GCE

## Quantitative Methods (MEI)

Unit G246: Decision Mathematics 1
Advanced Subsidiary GCE

## Mark Scheme for June 2015

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This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

OCR will not enter into any discussion or correspondence in connection with this mark scheme.

These are the annotations, (including abbreviations), including those used in scoris, which are used when marking

|  |  |
| :---: | :--- |
| $\checkmark$ and $\boldsymbol{x}$ | Meaning |
| BOD | Benefit of doubt |
| FT | Follow through |
| ISW | Ignore subsequent working |
| M0, M1 | Method mark awarded 0, 1 |
| A0, A1 | Accuracy mark awarded 0, 1 |
| B0, B1 | Independent mark awarded 0, 1 |
| SC | Special case |
| $\wedge$ | Omission sign |
| MR | Misread |
| Highlighting |  |
| Other abbreviations in mark scheme | Meaning |
| M1 dep* | Method mark dependent on a previous mark, indicated by * |
| cao | Correct answer only |
| oe | Or equivalent |
| rot | Rounded or truncated |
| soi | Seen or implied |
| www | Without wrong working |

Here are the subject specific instructions for this question paper
a Annotations should be used whenever appropriate during your marking.
The $A, M$ and $B$ annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks. It is vital that you annotate standardisation scripts fully to show how the marks have been awarded.

For subsequent marking you must make it clear how you have arrived at the mark you have awarded.
b An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct solutions leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly.

Correct but unfamiliar or unexpected methods are often signalled by a correct result following an apparently incorrect method.

Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, award marks according to the spirit of the basic scheme; if you are in any doubt whatsoever (especially if several marks or candidates are involved) you should contact your Team Leader.

The following types of marks are available.

## M

A suitable method has been selected and applied in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, eg by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

A
Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

## B

Mark for a correct result or statement independent of Method marks.
Unless otherwise indicated, marks once gained cannot subsequently be lost, eg wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.
d When a part of a question has two or more 'method' steps, the $M$ marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep *' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.

The abbreviation ft implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only - differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, exactly what is acceptable will be detailed in the mark scheme rationale. If this is not the case please consult your Team Leader.

Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.
f Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise. Candidates are expected to give numerical answers to an appropriate degree of accuracy, with 3 significant figures often being the norm. Small variations in the degree of accuracy to which an answer is given (e.g. 2 or 4 significant figures where 3 is expected) should not normally be penalised, while answers which are grossly over- or under-specified should normally result in the loss of a mark. The situation regarding any particular cases where the accuracy of the answer may be a marking issue should be detailed in the mark scheme rationale. If in doubt, contact your Team Leader.

Rules for replaced work
If a candidate attempts a question more than once, and indicates which attempt he/she wishes to be marked, then examiners should do as the candidate requests.

If there are two or more attempts at a question which have not been crossed out, examiners should mark what appears to be the last (complete) attempt and ignore the others.

NB Follow these maths-specific instructions rather than those in the assessor handbook.
$\mathrm{h} \quad$ For a genuine misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate's data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some units. This is achieved by withholding one A mark in the question.

Note that a miscopy of the candidate's own working is not a misread but an accuracy error.

| Question |  | Answer | Mark | Guidance |
| :---: | :---: | :---: | :---: | :---: |
| 1 | (i) | $791510426$ <br> 5 comparisons and 4 swaps | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \\ & \text { B1 } \\ & \text { [3] } \end{aligned}$ | Swapping 15 with 7 and then with 9 (list starts 79 ...) Correct list after first pass, if unclear take last list shown 5 comparisons and 4 swaps (both written, not tally marks) |
|  | (ii) | 749101526 <br> 2 comparisons and 1 swap | B1 <br> B1 <br> [2] | Correct list (after fourth pass), if unclear take last list shown 2 comparisons and 1 swap |
|  | (iii) | 15 | B1 [1] | 15 stated (cao) <br> $5+4+3+2+1$ (without 15) gets B0 |
|  | (iv) | $715926104$ <br> 1 comparison and 1 swap | B1 <br> B1 [2] | Correct list after first pass (must see all six values), if unclear take last list shown <br> 1 comparison and 1 swap (both written, condone a tally mark) |
|  | (v) | $791015264$ <br> 3 comparisons and 2 swaps | $\begin{aligned} & \text { B1 } \\ & \text { B1 } \\ & \text { [2] } \end{aligned}$ | Correct list after fourth pass (must see all six values), if unclear take last list shown 3 comparisons and 2 swaps (written, not tally marks) |
|  | (vi) | 5 comparisons and 5 swaps | $\begin{aligned} & \text { B1 } \\ & \text { [1] } \end{aligned}$ | Both written, not tally marks |
|  | (vii) | Shuttle sort, because it uses fewer than 15 comparisons <br> Know this because (any of): <br> - fourth pass only used 3 comparisons not the maximum of 4 <br> - 12 comparisons used <br> - 3 fewer comparisons <br> - with shuttle sort the number of comparisons on any pass is either the same as the number of swaps or is 1 more, so maximum number of comps possible in this case is 12 | M1 <br> A1 <br> [2] | Choosing shuttle and saying that it uses fewer comparisons (Note: 'more efficient' is in the question) <br> Evidence that candidate knows why shuttle uses fewer comparisons in this case, and is not just guessing Allow $4^{\text {th }}$ (or $3^{\text {rd }}$ ) pass does not need to shuttle all the way Allow comparisons must be at most $9+5$ (or $9+4$ or $9+3$ ) Allow comparisons at most 14 (or 13) <br> But NOT comparisons = 14 (or 13) |



\begin{tabular}{|c|c|c|c|c|}
\hline 3 \& (i) \& \begin{tabular}{l}
A: \((3.5,2) \Rightarrow P=9.5\) \\
\(B:(1.5,3) \Rightarrow P=10.5\) \\
(Optimum) vertex is \((1.5,3)\) \\
(Optimal) \(P=10.5\)
\end{tabular} \& M1
A1
A1
[3] \& \begin{tabular}{l}
Checking vertices (a correct calculation or a correct value for \(A\) or \(B\) ) or using a line of constant profit or equivalent (may be implied from optimum vertex or optimal \(P\) correct) \\
Identifying \((1.5,3)\) or B as optimum vertex, allow use of a star, arrow or underlining, condone not written in coordinate form Identifying 10.5 as optimal value, allow use of a star, arrow, underlining or 10.5 associated with \((1.5,3)\) or B in working, having already chosen this as the optimum vertex
\end{tabular} \\
\hline \& (ii) \& \((3,2)\) \& \[
\begin{aligned}
\& \text { B1 } \\
\& \text { [1] }
\end{aligned}
\] \& Need not be written in coordinate form, no working necessary \\
\hline \& (iii) \& \begin{tabular}{l}
Each (either) of the other points ( \(A\) and/or \(B\) ) have larger values for both \(x\) and \(y\) (and \(k>0\) so \(x+k y\) is bigger) \\
OR \\
(profit lines have negative slope but) lines joining \(D\) to \(A\) (or \(B\) ) and \(C\) to \(B\) (or \(A\) ) both have positive slope \\
\((1,0.5)\) to \((3.5,2)\) or \((1.5,3)\) and \((0.5,1.5)\) to \((3.5,2)\) or \((1.5,3)\) both have positive slope
\end{tabular} \& B1

[1] \& | Comparing the $x$ values and the $y$ values (imply referring to $k$ being positive or value of $x+k y$ or slope of profit lines) |
| :--- |
| Allow 'they ( $C$ and $D$ ) have smaller values of $x$ and $y$ ', provided answer refers (directly or indirectly) to both $C$ and $D$ as well as both $x$ and $y$ ' |
| OR 'profit line has negative gradient so crosses $C$ and $D$ first' NOT 'coordinates of $C$ and $D$ are smaller', 'these points are nearer to the origin', ' $x+k y$ is bigger at the other points' without further explanation |
| NOT descriptions about $y$ values only (e.g. ' $A$ and $B$ are higher up') | <br>

\hline \& (iv) \& $3.5+2 k>1.5+3 k \quad$ or using gradient of $A B=-\frac{1}{2}$ $\Rightarrow k<2$ \& M1
A1 \& Comparing $A$ and $B$ (for $k$ positive), may be implied from sight of 2 as a critical value (not just one of many trials) or $-1 / 2$ as a gradient $k<2$ (o.e.) seen as part of answer, allow $\leq$ <br>

\hline \& \& $$
\begin{aligned}
& 3.5+2 k>1+0.5 k \quad \text { or using gradient of } A D=\frac{3}{5} \\
& \Rightarrow k>-1 \frac{2}{3} \\
& {\left[\text { hence }-1 \frac{2}{3}<k<2\right]}
\end{aligned}
$$ \& M1

A1

[4] \& Comparing $A$ and $D$, may be implied from sight of $-5 / 3$ as a critical value (but not just as one of many trials) or $3 / 5$ as a gradient $k>-1 \frac{2}{3}$ (o.e.) seen as part of answer, allow $\geq$ $-5 / 3$, accept 3 sf or better, condone -1.66 . If -1.6 is seen with a possible dot or line above, bod recurring decimal (Ignore other working, e.g. $A$ and $C$ ) <br>
\hline
\end{tabular}




| (ii) | $\begin{aligned} & A-B-C-E \\ & A-B-D-G \end{aligned}$ | $\begin{aligned} & \text { B1 } \\ & \text { B1 } \\ & \text { [2] } \end{aligned}$ | This route (written forwards or backwards) (cao) This route (written forwards or backwards) (cao) |
| :---: | :---: | :---: | :---: |
| (iii) | Not all even vertices or (some) odd vertices or (any of) $B, C, E$ and $G$ odd Accept 'not Eulerian' or 'non-Eulerian' | B1 [1] | Stating that there is at least one odd order vertex <br> May give specific orders, but need to pick out (at least one of) $B, C$, $E$ and $G$ as causing the problem |
| (iv) | $B C=200$ $B E=280$ $B G=350$ <br> $E G=100$ $C G=180$ $C E=80$ <br> (total $=300)$ $($ total $=460)$ $($ total $=430)$ <br>    <br> Repeat $B C$ and $E G=300$  <br> Length of shortest route $=2200+300$ <br>  $=2500$ metres or 2.5 km   | B1 <br> M1 <br> A1 <br> [3] | Seeing at least four of these six paths and their lengths (or replace a pair of path weights by their sum) Do not imply this mark from answer <br> Selecting $B C$ and $E G$ (may be implied from answer 2500) <br> 2500 or 2.5 (units may be implied) |



| 6 | (i) | Cube 2 | B1 <br> [1] | Correct graph |
| :---: | :---: | :---: | :---: | :---: |
|  | (ii) | 2 | $\begin{aligned} & \hline \text { B1 } \\ & \text { [1] } \end{aligned}$ | (cao) |
|  | (iii) | Cube 4 | B1 <br> [1] | Adding arc YR, and no others Only need to check solid line |
|  | (iv) |  | M1 <br> A1 <br> [2] | (Six) arcs for cubes 2 and 4 added Only need to check solid lines <br> Labelling correct |



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