## Thursday 11 June 2015 - Afternoon

## GCSE METHODS IN MATHEMATICS

B392/02 Methods in Mathematics 2 (Higher Tier)

## Candidates answer on the Question Paper.

OCR supplied materials:
None
Other materials required:

- Scientific or graphical calculator
- Geometrical instruments
- Tracing paper (optional)


| Centre number |  |  |  |  |  | Candidate number |  |  |  |  |
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## INSTRUCTIONS TO CANDIDATES

- Write your name, centre number and candidate number in the boxes above. Please write clearly and in capital letters.
- Use black ink. HB pencil may be used for graphs and diagrams only.
- Answer all the questions.
- Read each question carefully. Make sure you know what you have to do before starting your answer.
- Your answers should be supported with appropriate working. Marks may be given for a correct method even if the answer is incorrect.
- Write your answer to each question in the space provided. Additional paper may be used if necessary but you must clearly show your candidate number, centre number and question number(s).
- Do not write in the bar codes.


## INFORMATION FOR CANDIDATES

- The number of marks is given in brackets [ ] at the end of each question or part question.
- Quality of written communication will be assessed in questions marked with an asterisk (*).
- The total number of marks for this paper is $\mathbf{9 0}$.
- This document consists of 20 pages. Any blank pages are indicated.



## Formulae Sheet: Higher Tier

Area of trapezium $=\frac{1}{2}(a+b) h$


Volume of prism $=($ area of cross-section $) \times$ length

In any triangle $A B C$
Sine rule $\quad \frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C}$
Cosine rule $a^{2}=b^{2}+c^{2}-2 b c \cos A$


Area of triangle $=\frac{1}{2} a b \sin C$

Volume of sphere $=\frac{4}{3} \pi r^{3}$
Surface area of sphere $=4 \pi r^{2}$


Volume of cone $=\frac{1}{3} \pi r^{2} h$
Curved surface area of cone $=\pi r l$


## The Quadratic Equation

The solutions of $a x^{2}+b x+c=0$,
where $a \neq 0$, are given by
$x=\frac{-b \pm \sqrt{\left(b^{2}-4 a c\right)}}{2 a}$

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Answer all the questions.

1 (a) Use your calculator to work out the following.
(i) $4.1 \times \sqrt{8^{3}}$
(a)(i)
(ii) $\frac{\left(1.6 \times 10^{2}\right) \times\left(9.7 \times 10^{8}\right)}{1.25}$
(ii)
(b) Andrea is working without a calculator. She does $1215 \div 6$ and gets the answer 22.5 .

Show the working for one way that Andrea could check her answer without using a calculator.
$\qquad$
$\qquad$
$\qquad$
(c) Write 1.3 as a fraction.
(c)

2 (a) In the diagram below, triangle $A B C$ has side $A C$ continued to $D$.


There are errors in the following proof.

```
w+x+y=18\mp@subsup{0}{}{\circ}}\mathrm{ (angle sum of a triangle is 180}\mp@subsup{}{}{\circ}\mathrm{ )
w+y+z=18\mp@subsup{0}{}{\circ}}\mathrm{ (angles on a straight line add up to 180}\mp@subsup{}{}{\circ}\mathrm{ )
So }w+x=
Exterior angle of a triangle is equal to the sum of the opposite interior angles.
```

Tick the box to show which line contains the first error.
$\square$ The first line
The third line

(b)* The diagram below consists of four straight lines. EF and GH are parallel.


Calculate angles $p$ and $q$, giving a geometrical reason for each step in your working.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

3 (a) Divide $£ 54$ in the ratio 2:7.
(a) $£$
£
(b) (i) Calculate $\frac{3}{4} \times 7$. Give your answer as a mixed number.
(b)(i)
(ii) What exact number does $\frac{3}{4} \times 7$ need to be multiplied by to give $\frac{3}{4}$ ?
(ii)
(c) Bernard's wage is $10 \%$ more than Carlotta's wage.

Work out the ratio of Bernard's wage to Carlotta's wage. Write the ratio in its simplest form using whole numbers.
(c)

4 The first five terms of a sequence are shown below.

$$
3,5,7,9,11
$$

(a) Write an expression for the $n$th term of the sequence.
(a)
(b)* 3 and 7 are both terms in the sequence.

The product of 3 and 7 is $3 \times 7=21$. 21 is also a term in the sequence.
Show that the product of any two terms in the sequence will also be a term in the sequence.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

5 Two positive numbers, $x$ and $y$, add up to make 8 .
(a) Write an equation to show this relationship between $x$ and $y$.
(a)
(b) On the grid below, draw a graph which shows all possible pairs of values of $x$ and $y$.

(c) It is also known that $y$ is three times $x$.

By drawing a suitable additional line on the grid, find the values of $x$ and $y$.
(c) $x$ $\qquad$ $y$

6 The diagram below shows a cube of side 6 cm .
Square holes, of side 2 cm , have been drilled through the cube, between the middles of pairs of opposite sides.


Find the volume of the shape that is left.
$\mathrm{cm}^{3}$ [4]

7 (a) Solve.

$$
4(x-6)=x
$$

(a)
(b) It is given that $R=\frac{P}{A^{2}}$.
(i) Calculate the value of $R$ when $P=36$ and $A=4$.
(b)(i)
(ii) Make $A$ the subject of the formula.
(ii)
(iii) Write down a possible pair of values of $P$ and $A$ so that $R=3.4 \times 10^{8}$.
(iii)

8 ABCD is a square.
A circle passes through all the points $A, B, C$ and $D$.
The centre of the circle is at the centre of the square.


The area of square $A B C D$ is $36 \mathrm{~cm}^{2}$.
Work out the radius of the circle.

9 Triangle PQR is right-angled at Q.
$P Q=3.6 \mathrm{~cm} . \mathrm{PR}=8.6 \mathrm{~cm}$.

(a) Calculate the size of angle P .
(a)
(b) Calculate the area of triangle PQR.
(b)
$\mathrm{cm}^{2}$ [2]

10 (a) Solve.

$$
2 x^{2}+5 x-3=0
$$

## (a)

[4]
(b) Write $\frac{1}{x-2}-\frac{1}{x+2}$ as a single fraction. Give your answer in its simplest form.
(b)
(c) (i) An identity in $x$ is given below. Find the values of $u$ and $v$.

$$
x^{2}+4 x+8=(x+u)^{2}+v
$$

(c)(i) $u=$
$v=$
(ii) Carlos thinks that $x^{2}+4 x+8$ is always bigger than 8 .

Find a value of $x$ which makes $x^{2}+4 x+8$ smaller than 8 .
(ii)

11 PQRS is a rectangle. $P Q=3 \mathrm{~cm} ; \mathrm{QR}=5 \mathrm{~cm}$.


T is a point on RS with RT $=x \mathrm{~cm}$.
The rectangle is folded along PT. S then lies on RQ.
Show that $x^{2}-6 x+9=x^{2}+1$ and hence find the value of $x$.
$12 y$ is inversely proportional to the square root of $x$. When $x=4, y=8$.
(a) Find $y$ when $x=25$.
(a)
(b) Find $x$ when $y=2$.
(b)

13 (a) Use the axes below to sketch the graph of $y=3 \cos x$.

(b) The graph of $y=x^{3}-4 x$ is shown below.

On the same axes, sketch the graph of $y=x^{3}-4 x+1$.


14 (a) JKLM is a parallelogram. MK is a diagonal of the parallelogram.
N and P are points on MK such that angle $\mathrm{JNM}=$ angle $\mathrm{LPK}=90^{\circ}$.


Not to scale

Prove that triangles JNM and LPK are congruent.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
(b) EFGH is a parallelogram. $\mathrm{HG}=8.4 \mathrm{~cm}, \mathrm{FG}=3.9 \mathrm{~cm}$ and angle $\mathrm{FGH}=55^{\circ}$.


Calculate the length of the diagonal FH.
(b)

15 O is the centre of a circle with radius 8 cm . $A$ and $B$ are points on the circle.
Angle AOB is $50^{\circ}$.
Calculate the perimeter of the shaded segment.


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