# GCSE Mathematics 

Foundation Tier Unit 3 Geometry and Algebra
Mark scheme

## 43603F

November 2015

Mark schemes are prepared by the Lead Assessment Writer and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all associates participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the students' responses to questions and that every associate understands and applies it in the same correct way. As preparation for standardisation each associate analyses a number of students' scripts. Alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, associates encounter unusual answers which have not been raised they are required to refer these to the Lead Assessment Writer.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of students' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

Further copies of this mark scheme are available from aqa.org.uk

## Glossary for Mark Schemes

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Mathematics papers, marks are awarded under various categories.

If a student uses a method which is not explicitly covered by the mark scheme the same principles of marking should be applied. Credit should be given to any valid methods. Examiners should seek advice from their senior examiner if in any doubt.

M

A

B
ft
oe
$[a, b]$
3.14 ...

Use of brackets

SC Special case. Marks awarded within the scheme for a common misinterpretation which has some mathematical worth.

Mdep A method mark dependent on a previous method mark being awarded.

Bdep A mark that can only be awarded if a previous independent mark has been awarded.
Method marks are awarded for a correct method which could lead to a correct answer.

Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied.

Marks awarded independent of method.
Follow through marks. Marks awarded for correct working following a mistake in an earlier step.

Or equivalent. Accept answers that are equivalent. eg, accept 0.5 as well as $\frac{1}{2}$

Accept values between $a$ and $b$ inclusive.

Accept answers which begin 3.14 eg 3.14, 3.142, 3.149.

It is not necessary to see the bracketed work to award the marks.

Examiners should consistently apply the following principles

## Diagrams

Diagrams that have working on them should be treated like normal responses. If a diagram has been written on but the correct response is within the answer space, the work within the answer space should be marked. Working on diagrams that contradicts work within the answer space is not to be considered as choice but as working, and is not, therefore, penalised.

## Responses which appear to come from incorrect methods

Whenever there is doubt as to whether a candidate has used an incorrect method to obtain an answer, as a general principle, the benefit of doubt must be given to the candidate. In cases where there is no doubt that the answer has come from incorrect working then the candidate should be penalised.

## Questions which ask candidates to show working

Instructions on marking will be given but usually marks are not awarded to candidates who show no working.

## Questions which do not ask candidates to show working

As a general principle, a correct response is awarded full marks.

## Misread or miscopy

Candidates often copy values from a question incorrectly. If the examiner thinks that the candidate has made a genuine misread, then only the accuracy marks (A or B marks), up to a maximum of 2 marks are penalised. The method marks can still be awarded.

## Further work

Once the correct answer has been seen, further working may be ignored unless it goes on to contradict the correct answer.

## Choice

When a choice of answers and/or methods is given, mark each attempt. If both methods are valid then M marks can be awarded but any incorrect answer or method would result in marks being lost.

## Work not replaced

Erased or crossed out work that is still legible should be marked.

## Work replaced

Erased or crossed out work that has been replaced is not awarded marks.

## Premature approximation

Rounding off too early can lead to inaccuracy in the final answer. This should be penalised by 1 mark unless instructed otherwise.

| $\mathbf{Q}$ | Answer | Mark | Comments |
| :--- | :---: | :---: | :---: |



| 2 | metres | B1 | Accept m |
| :---: | :---: | :---: | :---: |
|  | kilograms | B1 | Accept kg |
|  | litres | B1 | Accept l |
|  | Additional Guidance |  |  |
|  | Condone incorrect spelling provided intention is clear |  |  |


| Q | Answer | Mark | Comments |  |
| :---: | :---: | :---: | :---: | :---: |
| 3(a) $C D$ and $E F$ |  | B1 |  |  |
| 3(b) | $A B$ and $G H$ | B1 |  |  |
| 3(c) | $C D$ and $J K$ | B1 |  |  |
| 4(a) | 11 | B1 |  |  |
|  | $\mathrm{cm}^{2}$ | B1 |  |  |
|  | Additional Guidance |  |  |  |
|  | 11 cm |  |  | B1 B0 |
|  | $16 \mathrm{~cm}^{2}$ |  |  | B0 B1 |
|  | $\frac{11}{42}$ or 11 out of 42 |  |  | B0 B0 |
| 4(b) | Rectangle drawn with dimensions 8 by 1 <br> or 7 by 2 <br> or 6 by 3 <br> or 5 by 4 | B1 | Accept non-integer lengths if clear |  |
|  | Additional Guidance |  |  |  |
|  | Do not accept square drawn |  |  |  |
|  | Mark drawing |  |  |  |


| $\mathbf{Q}$ | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |




| $\mathbf{Q}$ | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |




| $\mathbf{Q}$ | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| 6 | 2 cm or 8 cm <br> or SF 4 seen or implied | B1 | Accept [1.9, 2.1] or [7.9, 8.1] |
| :---: | :---: | :---: | :---: |
|  | $\frac{\text { their } 8 \times 1.7}{\text { their } 2}$ | M1 | oe |
|  | 6.8 or 7 | A1 | Accept [6.4, 7.3] <br> SC1 for $3 \times 1.7=5.1$ |
|  | Additional Guidance |  |  |
|  | Beware 8 m is incorrect |  |  |



| 8 | Alternative method 1 |  |  |
| :---: | :---: | :---: | :---: |
|  | $\frac{45 \times 5}{8}$ or $28(.125)$ | M1 | $\frac{26 \times 8}{5}$ or 41.6 |
|  | 28.(125) <br> and 45 km longer seen or implied | A1 | 41.6 <br> and 45 km longer seen or implied |
|  | Alternative method 2 |  |  |
|  | $45 \div 8$ or 5.6 (25) and $26 \div 5$ or 5.2 | M1 | $8 \times 26 \text { or } 208$ <br> and $5 \times 45$ or 225 |
|  | 5.6(25) and 5.2 <br> and 45 km longer seen or implied | A1 | 208 and 225 <br> and 45 km longer seen or implied |


| $\mathbf{Q}$ | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| 9(a) | $35.25+65.5$ or 100.75 <br> or <br> $105-(35.25+65.5)$ <br> or <br> $105-$ their 100.75 | M1 | Condone missing bracket |
| :---: | :--- | :--- | :--- |
|  | 4.25 | A1 |  |


| 9(b) | One correctly evaluated trial of 5 ticket prices. | M1 | $\begin{aligned} & 4 \times 65.5+35.25=297.25 \\ & 3 \times 65.5+2 \times 35.25=267 \\ & 2 \times 65.5+3 \times 35.25=236.75 \\ & 65.5+4 \times 35.25=206.5 \\ & 5 \times 35.25=176.25 \end{aligned}$ |
| :---: | :---: | :---: | :---: |
|  | Adult 3 <br> Child 2 | A1 | $3 \times 65.5+2 \times 35.25$ chosen as answer |


| $\mathbf{Q}$ | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| 10 | Arc of radius 8 cm from left hand end of base or <br> arc of radius 10 cm from right hand end of base <br> or 160 m is 8 cm <br> or 200 m is 10 cm seen | M1 | tolerance $\pm 2 \mathrm{~mm}$ |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Arc of radius 8 cm from left hand end of base and arc of radius 10 cm from right hand end of base | M1 | tolerance $\pm 2 \mathrm{~mm}$ |  |
|  | Fully correct triangle with construction arcs shown | A1 | SC1 for 3 ${ }^{\text {rd }}$ vertex in tolerance |  |
|  | Additional Guidance |  |  |  |
|  | Condone restart with own 12 cm base |  |  |  |
|  | Fully correct triangle without construction arcs |  |  | SC1 |
|  | Triangle correct but reversed on base line |  |  | M1M1A0 |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| $\mathbf{1 1 ( a )}$ | $4 \times 4.5+3$ or 21 | M1 | $4(4 x+3)$ or $16 x+12$ |
| :--- | :--- | :---: | :--- |
|  | their $21 \times 4$ | M1dep | $16 \times 4.5+12$ |
|  | 84 | A1 |  |


| $\mathbf{1 1 ( b )}$ | $2 \times 15+30=60$ or $30+30=60$ | M1 |  |
| :--- | :--- | :---: | :--- |
|  | $3 \times 15+15=60$ or $45+15=60$ | M1 |  |
|  | States, shows or implies third angle <br> is 60 | Q1 | Strand (ii) <br> eg $180-60-60=60$ |


| 12 | $[38,42]$ | B1 | SC1 [218, 222] |
| :--- | :--- | :---: | :--- |
|  | $[038,042]$ | Q1 | Strand (i) for a three figure bearing |


| 13 | $360-(80+78+75)$ <br> or $360-233$ <br> or 127 | M1 | oe |
| :---: | :--- | :---: | :--- |
|  | $180-$ their 127 or 53 | M1dep | oe |
|  | $180-(53+53)$ or $180-106$ | M1dep | oe |
|  | 74 | A1 |  |


|  | $B(-1,4)$ | B2 | B1 for each coordinate |
| :---: | :--- | :---: | :--- |
| 14 | $D(-6,8)$ and $F(2,12)$ | B2 | B1 for each <br> or $D(-6, \ldots)$ and $F(2, \ldots)$ <br> or $D(\ldots, 8)$ and $F(\ldots, 12)$ |


| $\mathbf{Q}$ | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |

## Alternative method 1

| $10 \times 12$ or 120 <br> or $\frac{1}{2} \times 10 \times(18-12)$ <br> or 30 | M1 | oe |
| :--- | :--- | :--- |
| $10 \times 12$ or 120 <br> and $\frac{1}{2} \times 10 \times(18-12)$ <br> or 30 | M1 | oe |
| 150 | A1 |  |

## Alternative method 2

| $10 \times 18$ or 180 <br> or $\frac{1}{2} \times 5 \times(18-12)$ or 15 <br> or $\frac{1}{2} \times 5 \times(18-12) \times 2$ or 30 | M1 | oe |
| :--- | :--- | :--- |
| $10 \times 18$ or 180 | M1 | oe |
| and $\frac{1}{2} \times 5 \times(18-12) \times 2$ or 30 | A1 |  |
| 150 | M1 | oe |
| Alternative method 3 | M1 | oe |
| $\frac{1}{2}(12+18) \times 5$ | A1 |  |
| $\frac{1}{2}(12+18) \times 5 \times 2$ or 75 |  |  |
| 150 |  |  |


| $\mathbf{Q}$ | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |



| Q Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| 16(b) | Alternative method 1 |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Rotation | B1 |  |  |
|  | Origin or ( 0,0 ) or $O$ | B1 | oe |  |
|  | 180 (clockwise) <br> or 180 (anticlockwise) <br> or -180 | B1 | oe |  |
|  | Alternative method 2 |  |  |  |
|  | Enlargement and SF-1 | B2 |  |  |
|  | Origin or (0, 0) or $O$ | B1 | oe |  |
|  | Additional Guidance |  |  |  |
|  | Rotation, (0, 0), 90 then 90 |  |  | B1B1B0 |
|  | Accept 180C for 180 (clockwise) |  |  | B1 |
|  | Accept $1 / 2$ turn for 180 |  |  | B1 |
|  | Accept $\binom{0}{0}$ for origin |  |  | B1 |
|  | Enlargement (0, 0) |  |  | B0B1 |
|  | Allow rotate, rotating, rotational (symmetry) |  |  | B1 |
|  | Mixed transformations, eg translation of 180 reflection (0, 0) |  |  | $\begin{aligned} & \text { B0B0B1 } \\ & \text { B0B1B0 } \end{aligned}$ |
|  | Do not accept turn for rotation |  |  | B0 |
|  | Double transformations eg Rotate, translate |  |  | B0B0B0 |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| 17 | $\frac{12.5 \times 17.6 \text { or } 220}{}$ | M1 |  |
| :--- | :--- | :---: | :--- |
|  | $\frac{7(14+\text { their } 220)}{3}$ | M1dep |  |
|  | 546 or 546.00 | Q1 | Strand(i) |


| 18 | 1 gallon $=4.5$ litres stated or implied | B1 | eg their $144 \div 4.5$ |  |  |
| :---: | :--- | :---: | :---: | :---: | :---: |
|  | $40 \times 40 \times 90$ or 144000 | M1 |  |  |  |
|  | their $144000 \div 1000$ or 144 | M1dep |  |  |  |
|  | 32 | A1 |  |  |  |
|  | Additional Guidance |  |  |  | B1M1M1A1 |


| 19(a) | Alternate | B1 |  |
| :--- | :--- | :--- | :--- |


| $\mathbf{1 9}$ 19(b) | $12 x-60(=2 x+100)$ | B1 | Expanding brackets |
| :--- | :--- | :---: | :--- |
|  | $3(4 x-20)=2 x+100$ <br> or $12 x-$ their $60=2 x+100$ | M1 |  |
|  | $12 x-2 x=100+$ their 60 <br> or $10 x=160$ | M1dep | oe <br> Collecting terms |
|  | 16 | A1ft | ft their expansion |


| $\mathbf{Q}$ | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |

## Alternative method 1

| $\begin{gathered} 20 \\ \text { alt } 1 \end{gathered}$ | Alternative method 1 |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & \frac{1500}{600} \text { or } 2.5 \\ & \text { or } \frac{600}{1500} \text { or } 0.4 \end{aligned}$ | M1 | oe |  |
|  | $3.3 \times 2.5$ or 8.25 | M1 | $9.6 \div 2.5$ or 3.84 | $\begin{aligned} & \frac{15}{100} \times 9.6 \text { or } 1.44 \\ & \text { or } 0.85 \text { seen } \end{aligned}$ |
|  | $\frac{15}{100} \times 9.6 \text { or } 1.44$ <br> or 0.85 seen | M1 | $\begin{aligned} & \frac{15}{100} \times 3.84 \\ & \text { or } 0.576 \\ & \text { or } 0.85 \text { seen } \end{aligned}$ | $\begin{aligned} & 9.6-\text { their } 1.44 \\ & \text { or } 0.85 \times 9.6 \\ & \text { or } 8.16 \end{aligned}$ |
|  | $\begin{aligned} & 9.6 \text { - their } 1.44 \text { or } 8.16 \\ & \text { or } 0.0064 \times 0.85 \end{aligned}$ | M1dep | $\begin{array}{r} 3.84-0.576 \\ \text { or } 0.85 \times 3.84 \end{array}$ | their $8.16 \div 2.5$ |
|  | 8.25 and 8.16 | A1 | 3.26 or 3.264 or 3.27 |  |
|  | 1500 g pack identified | Q1ft | Strand(iii) correct conclusion for their values provided method marks have been awarded |  |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |

## Alternative method 2

| $3.3 \div 600$ or 0.0055 (price per 1g) | M1 | $3.3 \div 6$ or 0.55 (price per 100 g ) |  |
| :---: | :---: | :---: | :---: |
| $9.6 \div 1500$ or 0.0064 | M1 | $9.6 \div 15$ or 0.64 | $\begin{aligned} & 9.6 \times \frac{15}{100} \text { or } 1.44 \\ & \text { or } 0.85 \text { seen } \end{aligned}$ |
| $\frac{15}{100} \times 0.0064 \text { or } 0.00096$ <br> or 0.85 seen | M1dep | $\begin{aligned} & \frac{15}{100} \times 0.64 \text { or } \\ & 0.096 \\ & \text { or } 0.85 \text { seen } \end{aligned}$ | 9.6-1.44 <br> or $0.85 \times 1.44$ <br> or 8.16 |
| their 0.0064 - their 0.00096 <br> or $0.85 \times 0.0064$ <br> or 0.0054(4) | M1dep | $\begin{aligned} & \text { their } 0.64 \text { - their } \\ & 0.096 \\ & \text { or } 0.85 \times \text { their } 0.64 \\ & \text { or } 0.544 \end{aligned}$ | $8.16 \div 15$ or 0.544 |
| 0.0055 and 0.00544 | A1 | 0.55 and 0.544 |  |
| 1500 g pack identified | Q1ft | Strand(iii) correct conclusion for their values provided method marks have been awarded |  |


| $\mathbf{Q}$ | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |

## Alternative method 3



| $\mathbf{Q}$ | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| $\begin{gathered} 20 \\ \text { alt } 4 \end{gathered}$ | Alternative method 4 |  |  |
| :---: | :---: | :---: | :---: |
|  | $600 \div 3.3$ or 181.8... | M1 | $3.30 \times 5$ or 16.50 |
|  | $\begin{aligned} & \frac{15}{100} \times 9.6 \text { or } 1.44 \\ & \text { or } 0.85 \text { seen } \end{aligned}$ | M1 | $\frac{15}{100} \times 9.6 \text { or } 1.44$ <br> or 0.85 seen |
|  | $\begin{aligned} & 9.6-\text { their } 1.44 \\ & \text { or } 0.85 \times 9.6 \\ & \text { or } 8.16 \end{aligned}$ | M1 | $\begin{aligned} & 9.6-\text { their } 1.44 \\ & \text { or } 0.85 \times 9.6 \\ & \text { or } 8.16 \end{aligned}$ |
|  | $1500 \div$ their 8.16 or $183.8 \ldots$ | M1 | their $8.16 \times 2$ or 16.32 |
|  | 181.8... and 183.8 ... | A1 | 16.32 and 1650 |
|  | 1500 g pack identified | Q1ft | Strand(iii) correct conclusion for their values provided method marks have been awarded |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |

## Alternative method 1

| 7 or 28 seen | B1 |  |
| :--- | :---: | :--- |
| $2 \pi r=28$ <br> or $\pi d=28$ | M 1 | oe |
| $r=\frac{28}{2 \pi}$ <br> or $d=\frac{28}{\pi}$ <br> or $8.9 \ldots$ | M 1 | oe |
| $4.45(\ldots)$ or 4.46 | A 1 |  |
| 4.5 | B1ft | ft rounding their answer to 1 decimal place |

21
Alternative method 2

| 7 or 28 seen | B 1 |  |  |  |
| :--- | :---: | :--- | :---: | :---: |
| Correct trial using radius $=4$ | M 1 | $2 \times \pi \times 4=[25.12,25.14]$ |  |  |
| Correct trial using radius $=5$ | M 1 | $2 \times \pi \times 5=31.4 \ldots$ |  |  |
| $4.45(\ldots)$ or 4.46 | A 1 |  |  |  |
| 4.5 | B1ft | ft rounding their answer to 1 decimal place |  |  |
| Additional guidance |  |  |  |  |
| Accept 3.14 or better for pi for method marks | B1M1M1A0 <br> B1ft |  |  |  |
| Answer 8.9 from $28 \div \pi$ |  |  |  |  |

